

## Robot Dynamics

### Organizers & Chairs: Roy Featherstone, David Orin

#### Robot Dynamics: Equations and Algorithms

R. Featherstone<sup>1</sup> and D. E. Orin<sup>2</sup>

<sup>1</sup>University of Wales and <sup>2</sup>Ohio State University

#### Practical Models for Practical Flexible Arms

W. J. Book<sup>1</sup> and K. Obergfell<sup>2</sup>

<sup>1</sup>Georgia Institute of Technology and <sup>2</sup>Seagate Technology

- Reviews accomplishments in robot dynamics research
- Equations given for most important computations
- Recursive Newton-Euler, Composite-Rigid-Body, and Articulated-Body Algorithms
- Closed-loop systems & global analysis techniques discussed

```

for i = 1 to N do
    v_i = 'X_M^M_X_{\lambda(i)} v_{\lambda(i)} + h_i \dot{q}_i;
    a_i = 'X_M^M a_{\lambda(i)} + h_i \ddot{q}_i + h_i \dot{\ddot{q}}_i;
    f_i^J = I_i a_i + v_i \times I_i v_i - f_i^F
end
for i = N to 1 do
    r_i = h_i^T f_i^F;
    if \lambda(i) \neq 0 then f_{\lambda(i)}^J = f_{\lambda(i)}^J + \lambda(i) X_i^F f_i^J
end

```

#### Computational Robot Dynamics Using Spatial Operators

A. Jain and G. Rodriguez

California Institute of Technology

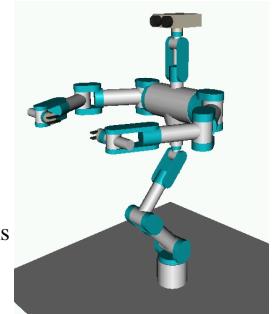
#### Operational Space Dynamics: Efficient Algorithms for Modeling and Control of Branching Mechanisms

Kyong-Sok Chang and Oussama Khatib

Stanford University

- Computational dynamics techniques for robotic systems
- A review of the Spatial Operator Algebra framework
- A look at standard dynamics problems, as well as novel ones, eg. diagonalized dynamics
- Open areas of research such as sensitivity analysis and optimization

- Branching Mechanisms
- Task/Posture Behavior Control
- Modified Spatial Notation
- Efficient Recursive O(n) Algorithms



#### Forward Dynamics Algorithms for Multibody Chains and Contact

D. K. Pai, U. M. Ascher and P. G. Kry

University of British Columbia

- Framework for derivation of forward dynamics algorithms.
- Formulate augmented matrix; block matrix elimination.
- Derives many algorithms: existing (ABM, CRBM) & new (contact evolution). Stability.
- Framework unifies many forward dynamics algorithms and contact evolution.

$$\left( \begin{array}{c|c} I & M_1 \\ \hline \times & I \\ \hline \times & \end{array} \right) \quad \Rightarrow \quad \left( \begin{array}{c|c} I & M_2 \\ \hline I & I \\ \hline \times & \end{array} \right)$$

$$\left( \begin{array}{c|c} I & \widehat{M}_1 \\ \hline I & I \\ \hline D_1 & \times \\ \hline I & \widehat{M}_2 \\ \hline I & I \\ \hline D_2 & \times \\ \hline I & \widehat{M}_3 \\ \hline I & I \\ \hline D_3 & \times \\ \hline \end{array} \right) \quad \Rightarrow \quad \left( \begin{array}{c|c} I & \widehat{M}_1 \\ \hline I & I \\ \hline D_1 & \times \\ \hline I & \widehat{M}_2 \\ \hline I & I \\ \hline D_2 & \times \\ \hline I & \widehat{M}_3 \\ \hline I & I \\ \hline D_3 & \times \\ \hline \end{array} \right)$$